

Problem 3.12

(a) Table of frequencies of the tones of the octave beginning with middle C, assuming that the A is above middle C is tuned to 440 Hz:

Note Name	C_4	C_4^\sharp	D_4	E_4^b	E_4	F_4	F_4^\sharp
Note Number	40	41	42	43	44	45	46
Frequency	262	277	294	311	330	349	370
Note Name	F_4^\sharp	G_4	G_4^\sharp	A_4	B_4^b	B_4	C_4
Note Number	46	47	48	49	50	51	52
Frequency	370	392	415	440	466	494	523

(b) Formula for frequency f as a function of the note number n :

$$f(n) = 440[2^{(\frac{n-49}{12})}]$$

(c) The spectrum has the form (frequency, amplitude) as:

$$[(-440, A_3), (-370, A_2), (-294, A_1), (294, A_1), (370, A_2), (440, A_3)]$$

The coefficients must have similar magnitudes, phases may be different to sound like a musical chord.

Spectrum plot :

